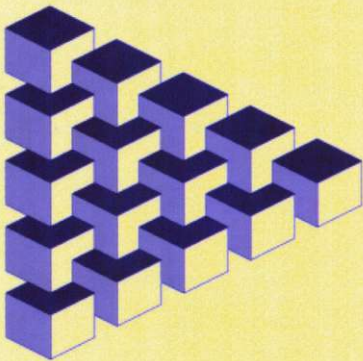


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# The IMO Compendium

A Collection of Problems  
Suggested for the  
International Mathematical  
Olympiads: 1959–2004



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# Contents

<b>Preface</b> .....	<b>v</b>
<b>1 Introduction</b> .....	<b>1</b>
1.1 The International Mathematical Olympiad .....	1
1.2 The IMO Compendium .....	2
<b>2 Basic Concepts and Facts</b> .. .. .	<b>5</b>
2.1 Algebra .....	5
2.1.1 Polynomials .....	5
2.1.2 Recurrence Relations .....	6
2.1.3 Inequalities .....	7
2.1.4 Groups and Fields .....	9
2.2 Analysis .....	10
2.3 Geometry .....	12
2.3.1 Triangle Geometry .....	12
2.3.2 Vectors in Geometry .....	13
2.3.3 Barycenters .....	14
2.3.4 Quadrilaterals .....	14
2.3.5 Circle Geometry .....	15
2.3.6 Inversion .....	16
2.3.7 Geometric Inequalities .....	16
2.3.8 Trigonometry .....	17
2.3.9 Formulas in Geometry .....	18
2.4 Number Theory .....	19
2.4.1 Divisibility and Congruences .....	19
2.4.2 Exponential Congruences .....	20
2.4.3 Quadratic Diophantine Equations .....	21
2.4.4 Farey Sequences .....	22
2.5 Combinatorics .....	22
2.5.1 Counting of Objects .....	22

<b>3</b>	<b>Problems</b>	<b>27</b>
3.1	IMO 1959	27
	3.1.1 Contest Problems	27
3.2	IMO 1960	29
	3.2.1 Contest Problems	29
3.3	IMO 1961	30
	3.3.1 Contest Problems	30
3.4	IMO 1962	31
	3.4.1 Contest Problems	31
3.5	IMO 1963	32
	3.5.1 Contest Problems	32
3.6	IMO 1964	33
	3.6.1 Contest Problems	33
3.7	IMO 1965	34
	3.7.1 Contest Problems	34
3.8	IMO 1966	35
	3.8.1 Contest Problems	35
	3.8.2 Some Longlisted Problems 1959-1966	36
3.9	IMO 1967	42
	3.9.1 Contest Problems	42
	3.9.2 Longlisted Problems	42
3.10	IMO 1968	51
	3.10.1 Contest Problems	51
	3.10.2 Shortlisted Problems	52
3.11	IMO 1969	55
	3.11.1 Contest Problems	55
	3.11.2 Longlisted Problems	55
3.12	IMO 1970	64
	3.12.1 Contest Problems	64
	3.12.2 Longlisted Problems	65
	3.12.3 Shortlisted Problems	72
3.13	IMO 1971	74
	3.13.1 Contest Problems	74
	3.13.2 Longlisted Problems	75
	3.13.3 Shortlisted Problems	81
3.14	IMO 1972	84
	3.14.1 Contest Problems	84
	3.14.2 Longlisted Problems	84
	3.14.3 Shortlisted Problems	89
3.15	IMO 1973	91
	3.15.1 Contest Problems	91
	3.15.2 Shortlisted Problems	92
3.16	IMO 1974	94
	3.16.1 Contest Problems	94
	3.16.2 Longlisted Problems	95

3.16.3	Shortlisted Problems	100
3.17	IMO 1975	103
3.17.1	Contest Problems	103
3.17.2	Shortlisted Problems	103
3.18	IMO 1976	106
3.18.1	Contest Problems	106
3.18.2	Longlisted Problems	106
3.18.3	Shortlisted Problems	112
3.19	IMO 1977	114
3.19.1	Contest Problems	114
3.19.2	Longlisted Problems	114
3.19.3	Shortlisted Problems	120
3.20	IMO 1978	123
3.20.1	Contest Problems	123
3.20.2	Longlisted Problems	123
3.20.3	Shortlisted Problems	128
3.21	IMO 1979	131
3.21.1	Contest Problems	131
3.21.2	Longlisted Problems	132
3.21.3	Shortlisted Problems	139
3.22	IMO 1981	143
3.22.1	Contest Problems	143
3.22.2	Shortlisted Problems	144
3.23	IMO 1982	147
3.23.1	Contest Problems	147
3.23.2	Longlisted Problems	148
3.23.3	Shortlisted Problems	153
3.24	IMO 1983	157
3.24.1	Contest Problems	157
3.24.2	Longlisted Problems	157
3.24.3	Shortlisted Problems	165
3.25	IMO 1984	169
3.25.1	Contest Problems	169
3.25.2	Longlisted Problems	169
3.25.3	Shortlisted Problems	176
3.26	IMO 1985	180
3.26.1	Contest Problems	180
3.26.2	Longlisted Problems	180
3.26.3	Shortlisted Problems	190
3.27	IMO 1986	193
3.27.1	Contest Problems	193
3.27.2	Longlisted Problems	194
3.27.3	Shortlisted Problems	201
3.28	IMO 1987	204
3.28.1	Contest Problems	204

3.28.2	Longlisted Problems . . . . .	204
3.28.3	Shortlisted Problems . . . . .	212
3.29	IMO 1988 . . . . .	216
3.29.1	Contest Problems . . . . .	216
3.29.2	Longlisted Problems . . . . .	217
3.29.3	Shortlisted Problems . . . . .	226
3.30	IMO 1989 . . . . .	231
3.30.1	Contest Problems . . . . .	231
3.30.2	Longlisted Problems . . . . .	232
3.30.3	Shortlisted Problems . . . . .	244
3.31	IMO 1990 . . . . .	249
3.31.1	Contest Problems . . . . .	249
3.31.2	Shortlisted Problems . . . . .	250
3.32	IMO 1991 . . . . .	254
3.32.1	Contest Problems . . . . .	254
3.32.2	Shortlisted Problems . . . . .	254
3.33	IMO 1992 . . . . .	259
3.33.1	Contest Problems . . . . .	259
3.33.2	Longlisted Problems . . . . .	259
3.33.3	Shortlisted Problems . . . . .	269
3.34	IMO 1993 . . . . .	272
3.34.1	Contest Problems . . . . .	272
3.34.2	Shortlisted Problems . . . . .	273
3.35	IMO 1994 . . . . .	277
3.35.1	Contest Problems . . . . .	277
3.35.2	Shortlisted Problems . . . . .	277
3.36	IMO 1995 . . . . .	281
3.36.1	Contest Problems . . . . .	281
3.36.2	Shortlisted Problems . . . . .	281
3.37	IMO 1996 . . . . .	286
3.37.1	Contest Problems . . . . .	286
3.37.2	Shortlisted Problems . . . . .	287
3.38	IMO 1997 . . . . .	292
3.38.1	Contest Problems . . . . .	292
3.38.2	Shortlisted Problems . . . . .	293
3.39	IMO 1998 . . . . .	297
3.39.1	Contest Problems . . . . .	297
3.39.2	Shortlisted Problems . . . . .	297
3.40	IMO 1999 . . . . .	302
3.40.1	Contest Problems . . . . .	302
3.40.2	Shortlisted Problems . . . . .	302
3.41	IMO 2000 . . . . .	307
3.41.1	Contest Problems . . . . .	307
3.41.2	Shortlisted Problems . . . . .	308
3.42	IMO 2001 . . . . .	312

4.33	Shortlisted Problems 1992	558
4.34	Shortlisted Problems 1993	568
4.35	Shortlisted Problems 1994	581
4.36	Shortlisted Problems 1995	589
4.37	Shortlisted Problems 1996	602
4.38	Shortlisted Problems 1997	618
4.39	Shortlisted Problems 1998	632
4.40	Shortlisted Problems 1999	646
4.41	Shortlisted Problems 2000	661
4.42	Shortlisted Problems 2001	675
4.43	Shortlisted Problems 2002	689
4.44	Shortlisted Problems 2003	701
4.45	Shortlisted Problems 2004	715
<b>A</b>	<b>Notation and Abbreviations</b>	<b>731</b>
A.1	Notation	731
A.2	Abbreviations	732
<b>B</b>	<b>Codes of the Countries of Origin</b>	<b>735</b>
	<b>References</b>	<b>737</b>